

3.9  
 (49)  $y = e^x$   
 $(0, 0)$   
 $y' = e^x$

## Opener

Non-Calculator

$$\frac{d}{dx}(xe^{\ln x^2}) = \cancel{x}^3$$

- (A)  $1+2x$       (B)  $x+x^2$       (C)  $3x^2$       (D)  $x^3$       (E)  $x^2+x^3$

$$f = x \quad g = e^{\ln x^2} \quad f' = 1 \quad g' = e^{\ln x^2} \cdot \left(\frac{1}{x^2}\right) \cdot 2x$$

$$e^{\ln x^2} + x e^{\ln x^2} \cdot \cancel{x}^2 = 3e^{\ln x^2}$$

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- 1) True or False. The derivative of  $y = 2^x$  is  $2^x$ . Justify your answer.  
 F  $y' = 2^x \cdot \ln 2$
- 2) True or False. The derivative of  $y = e^{2x}$  is  $2(\ln 2) e^{2x}$ . Justify your answer.  
 F  $y' = e^{2x} \cdot 2$
- 3) Which of the following is  $dy/dx$  if  $y = \tan(4x)$ ?  
 a)  $4 \sec(4x)\tan(4x)$       b)  $\sec(4x)\tan(4x)$       c)  $4 \cot(4x)$   
 d)  $\sec^2(4x)$       (D)  $4 \sec^2(4x)$        $y' = \sec^2(4x) \cdot 4$

## 3-8 Derivaves of the Inverse Trig Funcions

Learning Objecves:

I can calculate the derivaves of the inverse trig funcions

I can calculate the derivaves of inverse funcions given informaon about the funcion.

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## Derivaves of Inverse Trig Funcions

$$\begin{aligned} * \frac{d}{dx}(\sin^{-1} x) &= \frac{1}{\sqrt{1-x^2}} & * \frac{d}{dx}(\cos^{-1} x) &= -\frac{1}{\sqrt{1-x^2}} \\ * \frac{d}{dx}(\tan^{-1} x) &= \frac{1}{1+x^2} & \frac{d}{dx}(\cot^{-1} x) &= -\frac{1}{1+x^2} \\ \frac{d}{dx}(\sec^{-1} x) &= \frac{1}{|x|\sqrt{x^2-1}} & \frac{d}{dx}(\csc^{-1} x) &= \frac{-1}{|x|\sqrt{x^2-1}} \end{aligned}$$

## Ex1. Find the Derivave

$$1.) y = x^2 \sin^{-1} x \quad 2x \sin^{-1} x + \frac{x^2}{\sqrt{1-x^2}}$$

$$f' \cdot g + f \cdot g'$$

$$2.) y = \frac{\cos^{-1} x}{e^x} \quad \frac{\frac{-1}{\sqrt{1-x^2}}(e^x) - \cos'(x)(e^x)}{(e^x)^2}$$

$$\frac{f' \cdot g - f \cdot g'}{g^2}$$

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3.)  $y = \sin^{-1}(4x)$

$$y' = \frac{1}{\sqrt{1-(4x)^2}} \cdot 4$$

4.)  $y = \cos^{-1}\left(\frac{2}{x}\right)$

$$\begin{aligned} -\frac{2}{x^2} \cdot \frac{-1}{\sqrt{1-(2/x)^2}} &= \frac{2}{x^2 \sqrt{1-\frac{4}{x^2}}} \\ &= \frac{2}{x^2 \sqrt{\frac{x^2-4}{x^2}}} = x^2 \sqrt{\frac{x^2-4}{x^2}} = \frac{x^2 \sqrt{x^2-4}}{x^2} \\ &= \frac{2}{x \sqrt{x^2-4}} \end{aligned}$$

5.)  $y = \tan^{-1}(x^2 e^x)$

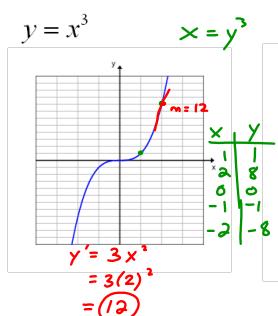
$$\frac{1}{1+(x^2 e^x)} \cdot (2x e^x + x^2 e^x)$$

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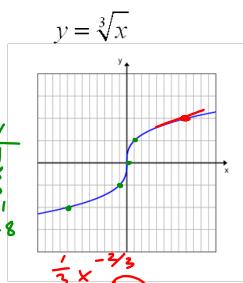
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### Inverse Functions

$y = f(x)$



$y = f^{-1}(x)$



Ex.1 Certain values of the function  $f(x)$  and its derivatives  $f'(x)$  are shown in the table below

x	f(x)	f'(x)
1	5	-3
2	1	-7
3	-8	-1/2

a.) Find  $\frac{d}{dx}(f^{-1}(x)) @ x=1$

$f'(2, 1) \rightarrow$

b.) Find the equation of the tangent line to  $y = f^{-1}(x)$  @  $x=1$

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### Homework

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